

Virtual element approximation of the Steklov eigenvalue problem

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ABSTRACT

In this work we develop a virtual element method for the two-dimensional Steklov eigenvalue problem. We propose a discretization by means of the virtual element method. Under standard assumptions on the computational domain, we establish that the resulting scheme provides a correct approximation of the spectrum and prove optimal order error estimates for the eigenfunctions and a double order for the eigenvalues. We also prove higher order error estimates for the computation of the eigensolutions on the boundary, which in some Steklov problems (computing sloshing modes, for instance) provides the quantity of main interest (the free surface of the liquid). Finally, we report some numerical tests supporting the theoretical results.

REFERENCES

- [1] Babuška I. and Osborn J. *Eigenvalue problems*, in *Handbook of Numerical Analysis*, Vol. II, P.G. Ciarlet and J.L. Lions, eds., North-Holland, Amsterdam, pp. 641–787 (1991).
- [2] Beirão da Veiga L., Brezzi F., Cangiani A., Manzini G., Marini L. D. and Russo A. Basic principles of virtual element methods. *Math. Models Methods Appl. Sci.* 23:199–214 (2013).
- [3] Bermúdez A., Rodríguez R. and Santamarina D. A finite element solution of an added mass formulation for coupled fluid-solid vibrations. *Numer. Math.* 87:201–227 (2000).
- [4] Canavati J. and Minsoni A. A discontinuous Steklov problem with an application to water waves. *J. Math. Anal. Appl.* 69:540–558 (1979).
- [5] Chiba M. Non-linear hydroelastic vibrations of a cylindrical tank with an elastic bottom containing liquid; Part II: linear axisymmetric vibration analysis. *J. Fluids Struct.* 7:57–73 (1993).